What is biological information?



Course 2: Biological codes

Thomas Lecuit

chaire: Dynamiques du vivant



- 1. General features of chemical information encoding and decoding
- 2. Case study 1: The genetic code
- 3. Case study 2: Transcriptional regulatory code
- 4. Case study 3: Signalling codes
- 5. Case study 4: Adhesion codes
- 6. Conclusions



Communication, Information, Codes in Humans

- Information is:
 - 1. Encoded
 - 2. Sent (sender)
 - 3. Transmitted (via electric signals)
 - 4. Interpreted (receiver)
- Information flows:









Samuel Morse (1791-1872)

• Information is:

- 1. Encoded
- 2. Sent (sender)
- 3. Transmitted (via electric signals)
- 4. Interpreted (receiver)
- A code is used as an *intermediate* between two forms of information
- A code *transforms* an information into another.
- In other words, a code changes a *representation* into another one.





Biological Information is mostly chemical

Reading and decoding information from the environment during chemotaxis



• Cells spend more time going up the gradient than down, so they go up the gradient



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R. Phillips, The Molecular Switch: signaling and allostery. *Princeton Univ. Press.* 2020

Reading and decoding information from the environment during chemotaxis



• **Specificity:** glucose, ribose, galactose, aspartate, serine

• Sensitivity

A ramp that increases the receptor occupancy by as little as 1 molecule/second (1 part in 600 Tar receptors/cell, or 0.0016) leads to a steady state increase in flagellar rotational bias by ~0.1).

This corresponds to a change in run length by a factor of ~3.

J. Segall, SM Block and & HC. Berg, *PNAS* 83, 8987-8991 (1986).

• Adaptation: resetting in a gradient and large amplitude



Information is mostly chemical

And based on molecular recognition: Metabolic pathways

Enzyme/substrate, Regulator/Enzyme









Information is mostly chemical



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And based on molecular recognition: Developmental Gene regulatory networks



L. Bodenstein. *Mechanisms of Development*, 162 (2020) https://doi.org/10.1016/j.mod.2020.103606



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1. The system and the observer/scientist:

- Information underlying the functioning of a system
- Information used to understand/model/represent a system

2. Operational definition of information:

- Information of a system is the set of parameters and prescriptions that allow an accurate prediction of the system's evolution, given a model.
- 3. What is relevant or useful information: (completeness vs sufficiency)

5. Can information be quantified?

- Yes (Shannon, courses #3 and 4) and Not yet (see courses #5 and 6)
- 6. Encoding and decoding information:
 - simplified (low dimensional) representation of relevant information



Mathematical theory of Information and Communication

- Claude Shannon 1948
- Key features of information theory:
 - semantic is not relevant
 - probabilistic nature of information
 - considers non uniform frequency of « events »

and statistics of the message



Claude Shannon (1916-2001)



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The Bell System Technical Journal Vol. XXVII July, 1948 No. 3

A Mathematical Theory of Communication

By C. E. SHANNON

INTRODUCTION

THE recent development of various methods of modulation such as PCM and PPM which exchange bandwidth for signal-to-noise ratio has intensified the interest in a general theory of communication. A basis for such a theory is contained in the important papers of Nyquist¹ and Hartley² on this subject. In the present paper we will extend the theory to include a number of new factors, in particular the effect of noise in the channel, and the savings possible due to the statistical structure of the original message and due to the nature of the final destination of the information.

The fundamental problem of communication is that of reproducing at one point either exactly or approximately a message selected at another point. Frequently the messages have *meaning*; that is they refer to or are correlated according to some system with certain physical or conceptual entities. These semantic aspects of communication are irrelevant to the engineering problem. The significant aspect is that the actual message is one *selected from a set* of possible messages. The system must be designed to operate for each possible selection, not just the one which will actually be chosen since this is unknown at the time of design.

If the number of messages in the set is finite then this number or any monotonic function of this number can be regarded as a measure of the information produced when one message is chosen from the set, all choices being equally likely. As was pointed out by Hartley the most natural choice is the logarithmic function. Although this definition must be generalized considerably when we consider the influence of the statistics of the message and when we have a continuous range of messages, we will in all cases use an essentially logarithmic measure.

The logarithmic measure is more convenient for various reasons:

1. It is practically more useful. Parameters of engineering importance

¹ Nyquist, H., "Certain Factors Affecting Telegraph Speed," *Bell System Technical Journal*, April 1924, p. 324; "Certain Topics in Telegraph Transmission Theory," A. I. E. E. Trans., v. 47, April 1928, p. 617.

² Hartley, R. V. L., "Transmission of Information," *Bell System Technical Journal*, July 1928, p. 535.

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Theory of Information and Communication

« The fundamental problem of communication is that of reproducing at one point either exactly or approximately a message selected at another point. »

• Basic architecture of *any* communication system





R. Phillips, The Molecular Switch: signaling and allostery. *Princeton Univ. Press.* 2020

• Information transfer in a noisy channel



What is relevant information?

Not all pixels in an image have the same relevance, ie. meaningfulness or usefulness



Recognition by components theory I. Biederman, *Psychological Review* 94, 115–147, 1987



What is relevant information?





I. Biederman, Psychological Review 94, 115–147, 1987



What is relevant biological information?

Table 1: Typical parameter values for a bacterial *E. coli* cell, the single-celled eukaryote S. cerevisiae (budding year and a narrange) and a particular of a particular backet and a contracteristic values for happily dividing cells of the common lab strains.

property	E. coli	budding yeast	mammalian (HeLa line)
cell volume	0.3–3 μm ³	30 – 100 μm ³	1,000–10,000 μm ³
proteins per μm ³ cell volume		2-4×10 ⁶	
mRNA per cell	10 ³ -10 ⁴	10 ⁴ -10 ⁵	10 ⁵ -10 ⁶
proteins per cell	~10 ⁶	~10 ⁸	~10 ¹⁰



2x10⁴

5x10⁶ bp

2x10³

ribosome

(A) bacterial cell (specifically, *E. coli*: $V \approx 1 \ \mu m^3$; $L \approx 1 \ \mu m$; $\tau \approx 1 \ hour$)

3x10⁶

DNA



(C) mammalian cell (specifically, HeLa: $V \approx 3000 \ \mu m^3$; $L \approx 20 \ \mu m$; $\tau \approx 1 \ day$)



>1000 different lipids

Figure 6: An order of magnitude census of of the three model cells we employ often book. A bacterial cell (E. coli), a unicellula yeast S. cerevisiae, and a mammalian ce



R. Milo and R. Phillips Cell Biology by the numbers. *Garland Science*

Liebmeister et al, R. Milo. PNAS (2013) doi/





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Figure 1: A Voconol itee diagram of the composition of an E. coll cell growing with a doubling time of 40 min. Each polygon area represents the relative fraction of the corresponding constituting in the composition of the

What is relevant biological information?

Genome by the numbers

Complexity does not scale with genome size/gene number

			1
organism	genome size (base pairs)	protein coding genes	number of chromosomes
model organisms			
model bacteria E. coli	4.6 Mbp	4,300	1
budding yeast S. cerevisiae	12 Mbp	6,600	16
fission yeast S. pombe	13 Mbp	4,800	3
amoeba D. discoideum	34 Mbp	13,000	6
nematode C. elegans	100 Mbp	20,000	12 (2n)
fruit fly D. melanogaster	140 Mbp	14,000	8 (2n)
model plant A. thaliana	140 Mbp	27,000	10 (2n)
moss P. patens	510 Mbp	28,000	27
mouse M. musculus	2.8 Gbp	20,000	40 (2n)
human H. sapiens	3.2 Gbp	21,000	46 (2n)
eukaryotes - multicellular			
pufferfish Fugu rubripes (smallest known vertebrate genome)	400 Mbp	19,000	22
poplar P. trichocarpa (first tree genome sequenced)	500 Mbp	46,000	19
corn Z. mays	2.3 Gbp	33,000	20 (2n)
dog C. familiaris	2.4 Gbp	19,000	40
chimpanzee P. troglodytes	3.3 Gbp	19,000	48 (2n)
wheat T. aestivum (hexaploid)	16.8 Gbp	95,000	42 (2n=бх)







What is relevant biological information?

Genome by bits

Genomic and chemical information is very large and dense



• Are all biological data/information meaningful to the system itself and to an observer to understand and predict its behaviour to specific endpoints?



- What are the relevant effective tuning variables?
 - Ex: cell actin cortex tension and material properties depend on 100s of proteins
 - few mechanical parameters such as stiffness and viscosity.
 - few molecules with key regulatory functions: MyosinII activation.



Information is mostly chemical

and based on protein affinity/molecular recognition

How to generate/produce a lot from little?

- Key feature: Balancing diversity and specificity Increasing diversity can impose a limit on coding system to ensure specificity
- Role of combinatorial properties to increase diversity
- Deterministic encoding vs Encoding in noising/stochastic dynamical systems
- 4 Case studies:
- tRNA/mRNA (genetic code): how to encode amino acid recruitment in protein synthesis?
- TF/DNA (regulatory code): how to encode gene expression of 10⁴ genes &cell state?
- Ligand/Receptor (signalling code): how to encode specific signalling responses?
- CAM/CAM (adhesion code): how to encode self-organisation of shapes from few 100 CAMs?



mRNA/tRNA-aminoacyl:

how to encode amino acid recruitment in protein synthesis?



Word code: codon Message: amino acid



Genetic information flow

ON PROTEIN SYNTHESIS

By F. H. C. CRICK

Medical Research Council Unit for the Study of Molecular Biology, Cavendish Laboratory, Cambridge

The importance of proteins

It is an essential feature of my argument that in biology proteins are uniquely important. They are not to be classed with polysaccharides, for example, which by comparison play a very minor role. Their nearest rivals are the nucleic acids. Watson said to me, a few years ago, 'The most significant thing about the nucleic acids is that we don't know what they do.' By contrast the most significant thing about proteins is that they can do almost anything. In animals proteins are used for structural purposes, but this is not their main role, and indeed in plants this job is usually done by polysaccharides. *The main function of proteins is to act as enzymes*. Almost all chemical reactions in living systems are catalysed by enzymes, and all known enzymes are proteins. It is at first sight paradoxical that it is probably easier for an organism to produce a new protein than to produce a new small molecule, since to produce a new small molecule one or more new proteins will be required in any case to catalyse the reactions.

I shall also argue that the main function of the genetic material is to control (not necessarily directly) the synthesis of proteins. There is a little

Ideas on Protein Synthesis (Oct. 1956)

The Doctrine of the Triad.

The Central Dogma: "Once information has got into a protein it can't get out again". Information here means the sequence of - the amino acid residues, or other sequences related to it. That is, we <u>may</u> be able to have



FH. Crick. Symp Soc. Exp. Biol. 12:138-163 (1958)



Discovery of the Genetic Code for Proteins

Proceedings of the NATIONAL ACADEMY OF SCIENCES

Volume 43 · Number 8 · August 15, 1957



ON THE IMPOSSIBILITY OF ALL OVERLAPPING TRIPLET CODES IN INFORMATION TRANSFER FROM NUCLEIC ACID TO PROTEINS

By S. Brenner

MEDICAL RESEARCH COUNCIL UNIT FOR THE STUDY OF THE MOLECULAR STRUCTURE OF BIOLOGICAL SYSTEMS, CAVENDISH LABORATORY, CAMBRIDGE, ENGLAND

Communicated by G. Gamow, June 10, 1957





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• Properties of the general overlapping triplet code:

Coding triplets from 4 nt: maximum of 64 triplets Each triplet shares 2 nt with next triplet. Degeneracy: 64 triplets degenerated in 20 aa.

- Therefore, peptide sequences would be constrained: There could not be more than 256 dipeptide sequences (represented by sequence of 4 nt).
 Yet there are in theory 400 dipeptide sequences.
- Proof based on data (*reductio ad absurdum*): 64 triplets are insufficient to code the known aa sequences.

Any triplet can be preceded (or succeeded) by only 4 different nucleotides, hence 4 different triplets.

Consider *j*,*k*,*l* aa. For every triplet for *k*, there are at most 4 *j* N-neighbour, and 4 *l*, C-neighbours. One can count the minimum of triplets required to encode *k* to account for the largest number of neighbours.

	Amino Acid	C-Neighbors	N-Neighbors	Minimum No. of Triplets Required	Amino Acid	C-Neighbors	N-Neighbor	Minimum No. of Triplets Required
	\mathbf{Lys}	18	17	5	Pro	13	12	4
	Ser	17	. 13	5	Tyr	12	10	3
	Gly	15	15	4	Glu	11	11	3
	Leu	15	15	4	Glun	12	9	3
	\mathbf{Cys}	15	14	4	Asp	10	11	3
	Arg	14	16	4	Asn	9	10	3
	Ala	14	15	4	Ileu	9	9	3
	Val	14	12	4	His	6	9	3
	Thr	13	14	4	Met	5	7	2
	Phe	13	14	4	Try	3	3	1
,					-		Г	otal 70

Discovery of the Genetic Code for Proteins



F. Crick, L. Barnett, S. Brenner and J. Watts_Tobin. Nature 192: 1227-1232 (1961)

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Discovery of the Genetic Code for Proteins

• The code is made of non overlapping triplets of bases



R. Phillips, J. Kondev, J. Thériot & H. Garcia. *Physical Biology of the Cell (Garland Science)* 2012



Proflavin leads to addition of base (+); or deletion of base (-)
 both give the *r* phenotype (no plague, *ie*. non functional T4 on *E*. *coli K* strain)

Results:

- + with reverts to wild type
- + with + or with maintain *r* phenotype
- +;+; + reverts to wild type

Table 1	1	DOTIFIE	MITTANT	WANTNO	mum	-	PHENOTYDE
Table 1		DOORPE	MUTANIS	HAVING	THE	T	LURNOLILE

- With -	+ \	With +
$\begin{array}{l} FC (1 + 21) \\ FC (23 + 21) \\ FC (1 + 23) \\ FC (1 + 9) \end{array}$	FC (0 + 58) FC (0 + 38) FC (0 + 40) FC (0 + 55) FC (0 + 54)	$\begin{array}{c} FC (40 + 57) \\ FC (40 + 58) \\ FC (40 + 55) \\ FC (40 + 54) \\ FC (40 + 38) \end{array}$

Table 3. TRIPLE MUTANTS HAVING A WILD OR PSEUDO-WILD PHENO-

TYPE FC (0 + 40 + 38) FC (0 + 40 + 58) FC (0 + 40 + 57) FC (0 + 40 + 54) FC (0 + 40 + 55)FC (1 + 21 + 23)

F. Crick, L. Barnett, S. Brenner and J. Watts_Tobin. Nature 192: 1227-1232 (1961)

Enraveling the genetic code

RNA Codewords and Protein Synthesis

The Effect of Trinucleotides upon the Binding of sRNA to Ribosomes

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MINUTES

Marshall Nirenberg and Philip Leder

To determine the minimum chain length of mRNA required for codeword recognition and to test the ability of chemically defined oligonucleotides to induce C^{14} -aminoacyl-sRNA binding to ribosomes, we have devised a rapid method of detecting this interaction and have found that trinucleotides are active as templates.



The trinucleotides, pUpUpU, pApApA, and pCpCpC, but not dinucleotides, direct the binding to ribosomes of phenylalanine-, lysine-, and proline-tRNA.





Marshall Nirenberg (1927-2010) Nobel 1968





Enraveling the genetic code

- Facts:
- Triplets of a 4 letter alphabet encode 23 amino acids
- Properties of the genetic code:
- Degeneracy
- Diversity
- Question: How can a molecular code withstand the impact of noise while accurately and efficiently translating information?





• Measurements of error rates

organism	errors per base or codon	BNID and measurement methods					
transc	ription						
E. coli	10 ⁻⁴	111146, transition mutations based on sequencing at very high (10 ⁶) coverage (2013)					
E. coli	10 ⁻⁵	105212, <i>in vitro</i> selection for rifampicin resistance and increased leakiness of an early, strongly polar nonsense mutation of lacZ (1983, 1986)					
E. coli	10 ⁻⁴	103453, activity in strains carrying lacZ mutations (1981)					
S. cerevisiae 2×10^{-6} S. cerevisiae 2×10^{-4}		110019, RNA pol II, determined <i>in vitro</i> (2008)					
		105213, RNA pol III, determined based on selectivity (2007)					
C. elegans	4×10^{-6}	4×10^{-6} 111144, determined using bar coded sequencing (2013)					
trans	lation						
E. coli	3 × 10 ⁻⁴	105069, Lys-tRNA, reporter system for frequency of each type of misreading error (2007)					
E. coli	$1-4 \times 10^{-3}$	105215, identify cases that do not contain the amino acid cysteine responsible for the missense substitution (1983)					
E. coli	10 ⁻⁴ -10 ⁻³	103454, identify cases that do not contain the amino acid cysteine responsible for the missense substitution (1977, 1983)					
B. subtilis	$4 imes 10^{-3}$	105466, GFP with nonsense mutation, also find 2.4% for frameshift (!) (2010)					
S. cerevisiae	$0.5-2 \times 10^{-5}$	105216, measurement of rescue rate of inactivating mutations of type III chloramphenicol acetyl transferase (1998)					

R. Milo and R. Phillips Cell Biology by the numbers. Garland Science



« During replication, the macroscopic replisome travels at a speed of 500 km/h, making a delivery of one of four coloured boxes on both sides of the street every 10 cm, completing its journey (for the case of bacterial replication) in 40 minutes. In this highly efficient delivery process, the truck would deliver a wrong package only once every 3 years! »

T. Baker R. Phillips The Molecular Switch. *Princeton Univ. Press*



• Kinetic Proofreading

Substrate C (resp. D) by recognition site c (resp.d):

k'c



John Hopfield (1933) Kinetic Proofreading: A New Mechanism for Reducing Errors in Biosynthetic Processes Requiring High Specificity (protein synthesis/DNA replication/amino-acid recognition)

J. J. HOPFIELD Department of Physics, Princeton University, Princeton, New Jersey 08540; and Bell Laboratories, Murray Hill, New Jersey 07974

Kinetic amplification of enzyme discrimination.

Jacques NINIO \diamond . The Salk Institute for Biological Studies P.O. Box 1809, San Diego, California 92112. (12-12-1974).

J.J. Hopfield (1974) *PNAS* (10): 4135–9 J. Ninio (1975). *Biochimie*. 57 (5): 587–95. $C + c \underset{k_{D}}{\rightleftharpoons} \operatorname{Cc} \rightarrow \operatorname{correct \ product} \quad K_{C} = k'_{C}/k_{C}$ $D + c \underset{k_{D}}{\rightleftharpoons} Dc \xrightarrow{W} \operatorname{error \ product} \quad K_{D} = k'_{D}/k_{D}$

• Equilibrium discrimination is not sufficient to account for measured error rates.

Error rate = $p_D/p_C = K_C/K_D = e^{-\beta\Delta E_{CD}}$ Energy difference scales with energy associated with formation of 1 H-bond: $\Delta \varepsilon \approx 2k_BT$ Error rate ~e⁻²~ 0.13 For measured error rate ~10⁻⁴

 $\Delta \varepsilon \approx -k_B T \ln 10^{-4} \sim 10 k_B T$



Kinetic Proofreading

- on rates are the same: $k'_{C} = k'_{D}$ So off rates carry the specificity (ie. discrimination).
- Minimum error attainable : $k_c/k_D = K_D/K_c \equiv f_0 = \exp (\Delta G_{CD}/RT)$
- Introduction of high energy intermediate Cc* produced by energy consuming driven reaction (ie. GTP hydrolysis) (2).
- Cc* dissociates more slowly than Dc*.
- Two stage kinetic model iterates the same discrimination. Assuming that *m*' is substrate independent and that $m' < k_C$ and $W < l_C$, (ie. reactions 1 and 2-3 are at near equilibrium) the error rate is:

$$f = f_{step1} \mathbf{x} f_{step2} = \frac{k_C}{k_D} \mathbf{x} \ l_C / l_D$$

If the same « reading » mechanism is used for dissociation from Cc* and Dc* as from Cc and Dc then: $f = f_o^2$

By adding *n* steps, discrimination is increased with error rate $f = f_o n+1$

J.J. Hopfield (1974) PNAS (10): 4135–9



 $C + c \underset{k_c}{\overset{k'c}{\rightleftharpoons}} Cc \xrightarrow{W} correct \text{ product } K_c = k'_c/k_c$ $D + c \underset{k_D}{\overset{k'_D}{\rightleftharpoons}} Dc \xrightarrow{W} \text{error product} \quad K_D = k'_D/k_D$





GDP+P+ Tu

• Kinetic Proofreading and translation

• The aminoacyl-tRNA is activated via GTP hydrolysis before incorporation to the aa chain (by EF-Tu in prokaryotes or eEF1A in eukaryotes).

> Tu·GTP·tRNA + A-site \leftarrow Tu·GTP·tRNA·A-site \leftarrow $tRNA \cdot A$ -site \rightarrow incorporation 2 1 tRNA + A-site

• Proofreading can also be interpreted as resulting from the introduction of a lag or delay (in step 2) that increases reading discrimination between correct and wrong codon/anticodon binding.



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J.J. Hopfield (1974) PNAS (10): 4135-9 R. Phillips The Molecular Switch. Princeton Univ. Press

• Kinetic Proofreading and translation

• There is a large excess (few 10 fold) of wrong tRNA-aa competing with a given correct tRNA-aa for binding to an anticodon.





- Error rate in the range of 10⁻⁴-10⁻⁶ /codon should inevitably produce proteins with the wrong amino acid in a cell: the average protein size is ~500aa in mammals, so expected translational error every 2000 average sized protein. There are 10¹⁰ proteins/cell, so there should be many proteins with wrong incorporated aa. But this is not the case.
- How does the cell cope with this given the impact on function?
- How to minimise this error-load?



• How can the genetic code withstand the impact of noise?

• Degeneracy of genetic code: many synonymous codons.

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There are potentially 64 different codons. The translation machinery cannot discern well between T and C in 3rd position of codon. Therefore the effective number of codons is at least 48. Since there are 23 aa, **the code shows degeneracy or redundancy**. All amino acids except methionine and

tryptophan are encoded by multiple codons (synonymous codons). Mutations are often synonymous.

- Carl Woese (1965) Hypothesis: Close-codons by sequence are either synonymous or encode amino-acids with similar chemical properties.
- Smoothness of code table reduces the *error-load* since misreading is likely to replace an amino acid by a chemically related one.



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T. Tlusty, Physics of Life Reviews 7 (2010) 362-376

- Hypothesis: The pattern and number of amino-acids are fundamental topological features of the noisy information channel that is embodied in the genetic code. (not a « frozen accident » F. Crick)
- Generic model of genetic code evolution: T. Tlusty, *Physics of Life Reviews* 7 (2010) 362–376
- Consider 3 features, or forces acting on fitness:
- Diversity: encoding functional proteins requires diverse set of aa. This tends to create a more heterogeneous code.
- Error load: evolutionary selection for codes that <u>minimize</u> the <u>deleterious</u> <u>impact of translation errors and mutations</u>. A mutation should have little impact on chemical nature of translated aa. Error-load selects for smooth code to reduce deleterious effect of mutations.
- Cost of coding system: cost of synthesizing molecules (material, energy and time)

 $fitness = -error-load + w_D \times diversity - w_C \times cost$

• Coding transition is governed mainly by the cost and quality of this information channel



• Coding transition is governed by properties of this information channel

 $fitness = -error-load + w_D \times diversity - w_C \times cost$



- Smootheness of code due to error-load tends to align vectors.
- Diversity tends to bring vectors in opposite directions.
- Cost brings disorder in vector orientations.

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 $p_{i\alpha}$ = probability that codon *i* matches amino acid α The N_C x N_A probabilities form a **code-matrix**. Initially the association is random and all $p_{i\alpha} = 1/N_A$ (no information in code): there is no information flow in the channel.

Evolution leads to correlations and information flow.

Code-matrix representation as the ensemble of N_C vectors in an N_A dimensional space. γ



Blue: codon encodes a single aa Green: codon encodes 2 aa Red: codon encodes 3 aa (no information)

T. Tlusty, Physics of Life Reviews 7 (2010) 362-376

• Coding transition is governed mainly by properties of this information channel

 $fitness = -error-load + w_D \times diversity - w_C \times cost$

- The optimal code is found by maximizing the fitness with respect to the code matrix $p_{i\alpha}$.
- When cost is large (large w_c), specificity is too costly, and the code-matrix is uniform. There is no code.
- When w_C is reduced below a critical value or correspondingly w_D is larger than critical value, certain codon have specificity for aa and there is a coding transition.
- The control parameter in the coding transition is the ratio of $w_{\rm D}$ and $w_{\rm C}$





How to produce a lot from little

- Key feature: Balancing specificity and diversity
 - Increasing diversity imposes a limit on the coding system to ensure specificity
 - The emergence of a smooth code is a solution for dealing with error-load
- Balanced by cost

 $fitness = -error-load + w_D \times diversity - w_C \times cost$



TF/DNA sequences:

how to encode gene expression of ~few 10⁴ genes from set of transcription factors (TFs)





- Organisms with more genes have more TFs.
- Proportion of genes coding TFs higher in more complex organisms:
- 169 TFs in yeast and 6275 genes: 2.5%
- 700 TFs in Drosophila and 13500 genes: 5%
- 1600 TFs in human, and 20.000 genes: 8%
- Yet: The number of transcription factors within super-families tends to be bounded
- The number of TFs in super-families correlates with degrees of freedom based on number of nucleotide sequences involved in TF binding (few 100s max).
- Organisms with more genes use superfamilies with larger set of TFs.



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Coding limits on the number of transcription factors

Shalev Itzkovitz^{1,2}, Tsvi Tlusty² and Uri Alon^{*1,2}

Table 1: Maximal numbers of transcription factors from each super-family in a single organism, and the organism in which the maximum is observed

	Super-family	Maximal # TFs	Kingdom	organism	Ρ	S	0	н	# sequence
I.	lambda repressor-like DNA-binding domains	77	A,B,E	Photorhabdus luminescens	3	Т	2	Т	64
2	C-terminal effector domain	88	A,B,E	Streptomyces avermitilis	-	-	-	-	-
3	srf-like	122	E	Arabidopsis thaliana	-	-	-	-	-
4	helix-loop-helix DNA-binding domain	186	E	Arabidopsis thaliana	2	1	1	2	128
5	DNA-binding domain	194	B,E	Oryza sativa	-	-	-	-	-
6	Zn2/Cys6 DNA-binding domain	246	E	, Fusarium graminearum	3	13	3	1	1,248
7	winged helix DNA-binding domain	299	A,B,E	Bordetella bronchiseptica	6	1	1	1	2,048
8	glucocorticoid receptor-like DNA-binding domain	376	A,B,E	C.elegans	2	9	3	2	3,456
9	homeodomain-like	417	A,B,E	Danio rerio	6	1	1	2	8.4*106
10	multi-domain C2H2 zinc fingers	1308	E	Mus musculus	6-30	1	1	Т	-



The kingdom in which each super-family is observed is abbreviated as A – Archea, B – Bacteria, E – Eukaryotes. Estimates for the number of possible sequences are shown (see methods). P – number of variable positions in each half-site, S – number of possible spacing between half-sites O – number of possible orientations, H – homo-dimers (1) or hetero-dimers (2). The number of sequences is $4^{p_{PH+}}O^{*}S/2$.

> alucocorticoid winged helix



homeodomain

S. Itzkovitz, T. Tulsty and U. Alon. BMC Genomics 2006, 7:239

Case Study 2: Transcriptional regulatory code

Model: Protein/DNA as noisy coding system

- Task: How to assign different sequences to each transcription factor (TF) in a way that avoids erroneous recognition in which a transcription factor binds the wrong sequence?
- Complexity and diversity of TFs: As an organism increases in complexity (eg. cell number, cell types and spatial temporal regulation), there is a need to increase the diversity of gene regulation, via the existence of new TFs.
- Limit on specificity: There is a risk that as the # of TFs increases, TFs will become increasingly similar and bind increasingly overlapping sequences. This will limit their specificity.
- This would thus tend to limit the number of TFs in an organism (similar to amino acids in cells)







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Case Study 2: Transcriptional regulatory code

Protein/DNA recognition: a Sphere-packing code.

Balancing Diversity and Specificity

The coding problem is akin to a sphere packing code in sequence space.

The size of the sphere of a given TF reflects the extent of binding to *adjacent* sequences

Increasing diversity will lead to overlapping spheres.

This leads to estimates of # of TFs in the same range as observations.

Table 2: Theoretical bounds for an n-length 4-letter code.

n	$\# \text{ code words} - 4^n/2$	Coloring bound	Sphere packing bound
3	32	18	3
4	128	42	9
5	512	95	32
6	2,048	210	107
7	8,192	460	372
8	32,768	994	1310

The sphere packing bounds are from equation (10). The coloring bound is given by equation (8).



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Diversity: +/-Specificity: ++





S. Itzkovitz, T. Tulsty and U. Alon. BMC Genomics 2006, 7:239

Case Study 2: Transcriptional regulatory code

Model: Protein/

• Hypothesis:

- Optimal coding theory predicts that over smooth coding: namely TFs with partially have similar/overlapping functions (regular minimise impact on fitness).

• Test:

- Measure *distance* between TFs based on *sequence bound*

-Measure *functional distance* (set of regulated genes and/or annotation)

About 14% (276/2016) of all TF pairs had significant target co-regulation. When considering pairs with similar binding sequences, the fraction with significant target co-regulation increases to over 50% (10/18, p-value of 5.1*10⁻⁵)





Transcription factors with overlapping binding sequences in S. cerevisae.

S. Itzkovitz, T. Tulsty and U. Alon. BMC Genomics 2006, 7:239

TF/DNA sequences:

how to encode gene expression of ~few 10⁴ genes from set of transcription factors (TFs)

Limits imposed on TF diversity in terms of optimal coding strategy.

Yet, there many other layers of regulation of transcription:

- Combinatorial effects and integration on regulatory sequences (see course #3).
- Introduces more degrees of freedom and alleviates constraints from sequence overlap





Case Study 2: Transcriptional regulatory code



O. Hobert Nature Neuroscience 22: 627-636. (2021)

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Spatial combinatorial encoding of cell identity: vertebrate neural tube

- In the developing vertebrate spinal cord, morphogenetic gradients establish regions of spatially subdivided transcription factor expression that promote cell fate.
- BMP secreted from the roof plate promotes specification of **dorsal sensory interneurons**, while secretion of Sonic Hedgehog (Shh) from the floor plate specifies **motoneuron/ventral interneuron fate**

BMP







Malin and Desplan C. *PNAS* 2021 Vol. 118 No. 28 e2101823118 (T. Jessel and J. Briscoe labs)

Temporal combinatorial encoding of cell identity: Drosophila nervous system

- In the Ventral Nerve Chain (VNC) distinct neurons are produced in each segment of the embryo
- Progenitor cells divide asymmetrically to generate a new progenitor and a neutron or a GMC which produces 2 neurons or glial cells.
- A temporal cascade of TFs and spatial cues encode cell identity.





C. Doe Annu. Rev. Cell Dev. Biol. 2017. 33:219-40



Case Study 2: Transcriptional regulatory code

Temporal combinatorial encoding of cell identity: Drosophila nervous system

- 60.000 neurons in the *Drosophila* visual system (²/₃ of the brain).
- Visual system requires the specification of distinct neurons.
- 100 Medulla neurons are specified from the Outer Proliferation Center (OPC), in a wave.
- Each progenitor generates a clonal descent of medulla neurons organised in a column.



Malin and Desplan C. PNAS 2021 Vol. 118 No. 28 e2101823118C.



Case Study 2: Tran

Temporal combinatorial end



system

- A temporal cascade to TFs encode distinct cell types.
- This is amplified by spatial cues in the outer proliferation center (OPC).
- Notch signalling amplifies cell diversification (binary choice).

X. Li et al., and C. Desplan. Nature 498, 456–462 (2013).











Ligand/Receptor (signalling code):

how to encode specific signalling output behaviours from different ligands?





There is a **limited set of signalling pathways in metazoans**: 7 BMP, Wnt, Hh, FGF and other RTKs (Receptor Tyrosine Kinase), JNK, TLRs, GPCRs.

- Ligands/Receptors (L/R) binding trigger specific cellular outputs.
- Paradox: Ligands and receptors are generally expressed in poorly restricted domains, yet their function is highly restricted in space and time.
- How is specificity achieved? What is the signalling encoding strategy?
- quantitative control.
- subcellular specification (context dependency)
- ligand diversification

1 to 1 L/R binding
Specific encoding

Promiscuous L/R binding (many to many) **Combinatorial encoding**





>>Power and Limits of these different strategies

- BMP signalling pathway
- Promiscuous L/R Interactions can be analyzed in terms of multi-dimensional L and R spaces.



Combinatorial Signal Perception in the BMP Pathway

Yaron E. Antebi,¹ James M. Linton,¹ Heidi Klumpe,^{1,2} Bogdan Bintu,¹ Mengsha Gong,¹ Christina Su,¹ Reed McCardell,¹ and Michael B. Elowitz^{1,3,4,*}

- Combinatorial sensing of BMP ligands.
- Reports BMP signalling with fluorescent reporter using BMP responsive element



Y.E. Antebi et al. and M.B. Elowitz. Cell 170, 1184-1196 (2017)



- The combinatorial logic of BMP ligands
- Binary interaction among BMP ligands reveals different classes of quantitative response behaviours



Y.E. Antebi et al. and M.B. Elowitz. Cell 170, 1184–1196 (2017)



Α

- A mathematical models recapitulates the computational properties of BMP signalling
- Two features are used to assess signalling computation and response profiles across 100.000 parameter sets.

 Relative ligand strength to quantify asymmetry in signalling (activity ratio btw weaker and stronger ligands, equal =1, asymmetry = 0).
 Ligand interference coefficient (+ or interactions)

• 4 core integration modes or classes of computations emerge: additive (addition), imbalance (subtraction), balance (multiplication) and ratiometric (division) signalling.

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Y.E. Antebi et al. and M.B. Elowitz. Cell 170, 1184–1196 (2017)

- The 4 computational modes arise through the interplay between different binding affinities (allowing competition for L/R binding) and existence of different complex activities.
- Additive: the 2 ligands have ~equivalent activities (ε_{i1k} ~ ε_{i2k})
- Ratiometric: signaling complexes from one ligand have higher activities than from the other ($\epsilon_{i1k} \ll \epsilon_{i2k}$)
- Imbalance: each receptor preferentially binds to a distinct ligand with which it forms a less active complex
- Balance: each receptor preferentially binds to the ligand with which it forms a more active complex

Y.E. Antebi et al. and M.B. Elowitz. *Cell 170*, 1184–1196 (2017)





- If only 1 ligand it signals from both receptors
- If 2 ligands, sorting among different receptors and lower total signalling

- Different cell types exhibit different computations.
- Receptors are expressed at different levels in different cell types.
- Receptor expression levels control computation in silico:

 – change R levels while fixing parameters constant. Some parameters produce few integration modes (left), while others are more versatile and generate different computations (right).

• Receptor expression levels affect computation in vivo: additive to radiometric or vice versa, imbalance to additive.



Y.E. Antebi et al. and M.B. Elowitz. Cell 170, 1184–1196 (2017)



- Combinatorial signal encoding has following properties:
- Sensitivity to absolute and relative concentrations.
- This increases the robustness to variations that affect all ligands in a correlated way (cell surface/cell size or shape, ligand accessibility, etc)
- Computation is integrated with ligand sensing, and emerges because of decoupling between binding and activity.
- Computational plasticity: can be tuned eg. by receptor levels.

See also: Su et al., and YE. Antebi, MB. Elowitz Cell Systems 13, 408–425 (2022) Ligand-receptor promiscuity enables cellular addressing

These interactions allow ligand combinations to selectively activate, or "address," individual cell types or groups of cell types based on their combinatorial receptor expression profiles.



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CAM/CAM (adhesion code):

how to encode self-organisation of shapes from few 100 Cell Adhesion Molecules





- Interpret cellular affinities in terms of molecular structure and organisation
- Cell surface selective adhesiveness underlies cell clustering during development
 - Specificity: correspondance and mutual fitting between 2 properties Can be resolved in terms of molecular theory

THE PROBLEM OF SPECIFICITY IN GROWTH AND DEVELOPMENT* PAUL WEISS YALE JOURNAL OF BIOLOGY AND MEDICINE

SIGNIFICANCE OF THE CELL MEMBRANE IN EMBRYONIC PROCESSES

By JOHANNES HOLTFRETER* Biology Department, University of Rochester, Rochester, N. Y.









Johannes Holtfreter 1901- 1992



• Encoding tissue organisation via cell-cell adhesion energy

Reconstruction of Tissues by Dissociated Cells

Some morphogenetic tissue movements and the sorting out of embryonic cells may have a common explanation.

2 August 1963, Volume 141, Number 3579 Malcolm S. Steinberg SCIENCE



Fig. 2. Hans Holtfreter pronouncing his disagreement with the experimental evidence of Mal Steinberg (shown here laughing) for the thermodynamic model of cell sorting. This photograph was taken at the embryology course at the Marine Biology Laboratory at Woods Hole, 1971.

Steinberg & Gilbert J. Exp. Zool. 2004, about Townes & Holtfreter J. Exp. Zool. 1955



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While the *adaptedness* brought about through evolution appears complex, the adaptiveness which makes evolution possible is born of simplicity. The entire genetic code (and more) is expressible with an alphabet containing only four elements. It would appear that a not inconsiderable amount of the "information" required to produce, through morphogenetic movement, the anatomy of a body part may be expressed in a code whose sole element is quantity: more versus less. There is, I think, reason to expect that as more realms of biological specificity yield to analysis, their most impressive feature may be the simplicity of the terms in which specificity-information, if you will—can be expressed (34).

Steinberg MS. Science. 141:401-408. 1963

Differential adhesion hypothesis accounts for cell sorting in vitro



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Based on D. Duguay, R. Foty and MS. Steinberg. Developmental Biology. 253: 309-323 (2003)

Differential adhesion hypothesis accounts for cell sorting



Interfacial Energy: It is the amount of reversible work to change the surface dE = k dS

Surface tension *k* (N/m):

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 derives from free energy difference between interface and bulk.

 – consequence of net inward intermolecular force at interface. Cell sorting in 3D



Based on R.Foty et al and MS. Steinberg Development 122:1611-1620 (1996)



Differential adhesion hypothesis accounts for cell sorting: Drosophila retina









- Chemoaffinity model of nerve routing: Sperry 1963
- Area-code hypothesis: Hood & Dreyer 1977, 1998
- Selective stabilisation by activity: Changeux 1976
- Recognition for synapse specificity? Reviewed in Sanes JR, Zipursky SP. Cell. 181(3):536-556 (2020)

CHEMOAFFINITY IN THE ORDERLY GROWTH OF NERVE FIBER PATTERNS AND CONNECTIONS*

BY R. W. SPERRY

DIVISION OF BIOLOGY, CALIFORNIA INSTITUTE OF TECHNOLOGY

R.W. Sperry. PNAS 50(4): 703-710 (1963)

The area code hypothesis revisited: Olfactory receptors and other related transmembrane receptors may function as the last digits in a cell surface code for assembling embryos

William J. Dreyer* Division of Biology, California Institute of Technology, Pasadena, CA 91125

WJ. Dreyer *PNAS* 95:9072–9077 (1998)





ABSTRACT Recent evidence emerging from several laboratories, integrated with new data obtained by searching the genome databases, suggests that the area code hypothesis provides a good heuristic model for explaining the remarkable specificity of cell migration and tissue assembly that occurs throughout embryogenesis. The area code hypothesis proposes that cells assemble organisms, including their brains and neryous systems, with the aid of a molecular-addressing code that functions much like the country, area, regional, and local portions of the telephone dialing system. The complexity of the information required to code cells for the construction of entire organisms is so enormous that we assume that the code must make combinatorial use of members of large multigene families. Such a system would reuse the same receptors as molecular digits in various regions of the embryo, thus greatly reducing the total number of genes required. We present the hypothesis that members of the very large families of olfactory receptors and vomeronasal receptors fulfill the criteria proposed for area code molecules and could serve as the last digits in such a code. We discuss our evidence indicating that receptors of these families are expressed in many parts of developing embryos and suggest that they play a key functional role in cell recognition and targeting not only in the olfactory system but also throughout the brain and numerous other organs as they are assembled.



- Large families with highly specific binding: not a synapse identification code but a code for self/ non-self recognition.
 - Dscam1 (fly): >18.000 splicing isoforms that differ within 3 lg domain. Isoform specific homophonic recognition. Each neuron expresses 10-40 isoforms in a probabilistic way.
 - Pcdh (vertebrates): 3 tandem genes (58 in total), that multimerize in cis and trans (model: size dependent recognition mechanism)



0

Strong No binding

- Small families with promiscuous binding for subtype recognitions. Ex: DIP/Dpr
- Combinatorial expression. Provides general address code.
- Reuse: to minimise size of families.

Reviewed in Sanes JR, Zipursky SL. Cell. 181(3):536-556 (2020)



Case Study 4: Limits of Cell adhesion code

Differential sorting of growth cones without target code recognition

Neural superposition

Axonal self-sorting without target guidance in *Drosophila* visual map formation

Egemen Agi¹†, Eric T. Reifenstein²†, Charlotte Wit¹, Teresa Schneider¹, Monika Kauer¹, Melinda Kehribar¹, Abhishek Kulkarni¹, Max von Kleist²*, P. Robin Hiesinger¹*

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- Growth cones show biased stochastic search with significant overlap
- Growth cones search is independent of target cell
- Self-organised filopodia meshwork based on neighbour interactions





E. Agi et al and R. Hiesinger *Science*. 2024 Mar 8;383(6687):1084-1092 M. Langen et al and R. Hiesinger. *Cell*. 2015 Jul 2;162(1):120-33

- Genetic code: deterministic, requires mechanisms for error minimisation (proofreading and « smooth encoding »)
- Transcriptional code: smooth encoding, but also combinatorial encoding and integration relaxes constraints on 1-to-1 specificity, and increases repertoire of context-dependent regulation.
- Signalling code: Promiscuous binding and combinatorial encoding increase cellular addressing compared to 1-to-1 L/R signalling. Also allows signal computation.
- Adhesion code: biased stochastic processes rather than deterministic encoding. Many small contribution rather than few, selective, deterministic molecular codes.



Some features of biological encoding

- Coding theory provides a framework to understand constraints on code evolution (error load, diversity and cost). Smooth encoding.
- **Combinatorial encoding** increases specific « addressing » (cell identity, cell responses)
- Deterministic use of code: genetic code
- Stochasticity and Algorithmic encoding: more consistent with self-organisation.
 - Random search and stabilisation of final configuration based on energy minimisation (DAH)
 - Biased stochastic search and final stabilisation by target (neural superposition).

THE VARIETY OF CONTENTS COMPRESSED IN THE MINIATURE CODE

It has often been asked how this tiny speck of material, the nucleus of the fertilized egg, could contain an elaborate code-script involving all the future development of the organism. A well-ordered association of atoms, endowed with sufficient resistivity to keep its order permanently, appears to be the only conceivable material structure that offers a variety of possible ('isomeric') arrangements, sufficiently large to embody a complicated system of 'determinations' within a small spatial boundary. Indeed, the number of atoms in such a structure need not be very large to produce an almost unlimited number of possible arrangements. For illustration, think of the Morse code. The two different signs of dot and dash in well-ordered groups of not more than four allow of thirty different specifications. Now, if you allowed yourself the use of a third sign, in addition to dot and dash, and used groups of not more than ten, you could form 88,572 different 'letters'; with five signs and groups up to 25, the number is 372,529,029,846,191,405

